









•	various ways to compromise the PRNG's state
	 cryptanalytic attacks
	 between receiving input samples the PRNG works as a stream cipher
	 a cryptographic weakness in this stream cipher might be exploited to recover its internal state
	- side-channel attacks
	 additional information about the actual implementation of the PRNG may be exploited
	 example: measuring the time needed to produce a new output may leak information about the current state of the PRNG (timing attacks) x = MD5(seed);
	seed = seed+1; // increment needs m+1 byte additions if the last m bytes are all 0xFF return x; // long output time \rightarrow last couple of bytes of seed are 0x00
	- input-based attacks
	 known-input attacks: an attacker is able to observe (some of) the PRNG inputs chosen-input attacks: an attacker is able to control (some of) the PRNG inputs typically applicable against smart cards
	 mishandling of seed files







	Attacks on X9.17
	 weaknesses leading to state compromise extensions part of the state (K) never changes if K is compromised, then the PRNG can never fully recover seed_{i+1} depends on seed_i only via output_i if K is known from a previous state compromise and output_i is observable, then finding seed_{i+1} is not so difficult (timestamps can usually be assumed to have only 10-20 bits of entropy)
	 deriving the seed from two consecutive outputs (and K) seed_{i+1} = E_K(T_i ⊕ output_i) (1) seed_{i+1} = D_K(output_{i+1}) ⊕ T_{i+1} (2)
ANST X9.17	 assume that timestamps has 10 bits of entropy try all values for T_i, and form a sorted list of possible values for seed_{i+1} using (1) try all values for T_{i+1}, and form another sorted list of possible values for seed_{i+1} using (2) the correct seed_{i+1} value is the one that appears on both lists (expected number of matching pairs is ~1+2²⁰⁻ⁿ)
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	ntropy accumulator
•	 inputs from each source are fed alternately into two entropy pools fast pool provides frequent reseeds ensures that state compromises has as short a duration as possible slow pool rare reseeds entropy is estimated very conservatively rationale: even if entropy estimation of the fast pool is inaccurate, the PRNG
•	still eventually gets a secure reseed from the slow pool
	 entropy of each sample is measured in three ways: a: programmer supplies an estimate for the entropy source
	 b: a statistical estimator is used to estimate the entropy of the sample c: length of the sample multiplied by ¹/₂
	 entropy estimate of the sample is min(a, b, c)
	 entropy contribution of a source is the sum of entropy estimates of all samples collected so far from that source
	- entropy contribution of each source is maintained separately
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	Reseed mechanism
	• reseed from the fast pool (h is SHA1, E is 3DES): $v_0 := h(fast pool)$ $v_i := h(v_{i-1} v_0 i)$ for $i = 1, 2,, P_t$ $K := h'(h(v_{Pt} K), k)$ $C := E_K(0)$ where h' is a "size adaptor" $h'(m, k) = first k bit of s_0 s_1 s_2 $ $s_0 = m$ $s_i = h(s_0 s_{i-1})$ $i = 1, 2,$ reset all entropy estimates to 0 wipe the memory of all intermediate values
Yarrow-160	 reseed from the slow pool: feed h(slow pool) into fast pool reseed from fast pool as described above [®] Levente Buttyán







Summary
 PRNGs for cryptographic purposes needs special attention simple congruential generators are predictable naïve PRNG design will not do (cf. early Netscape PRNG) widely used cryptographic PRNGs may have weaknesses too ANSI X9.17 DSA PRNG RSAREF 2.0 some guidelines for using vulnerable PRNGs design of Yarow-160 careful design that seems to resist various attacks protecting the entropy pools
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