

# Message authentication and authenticated encryption

*Security Protocols (bmevihim132)*

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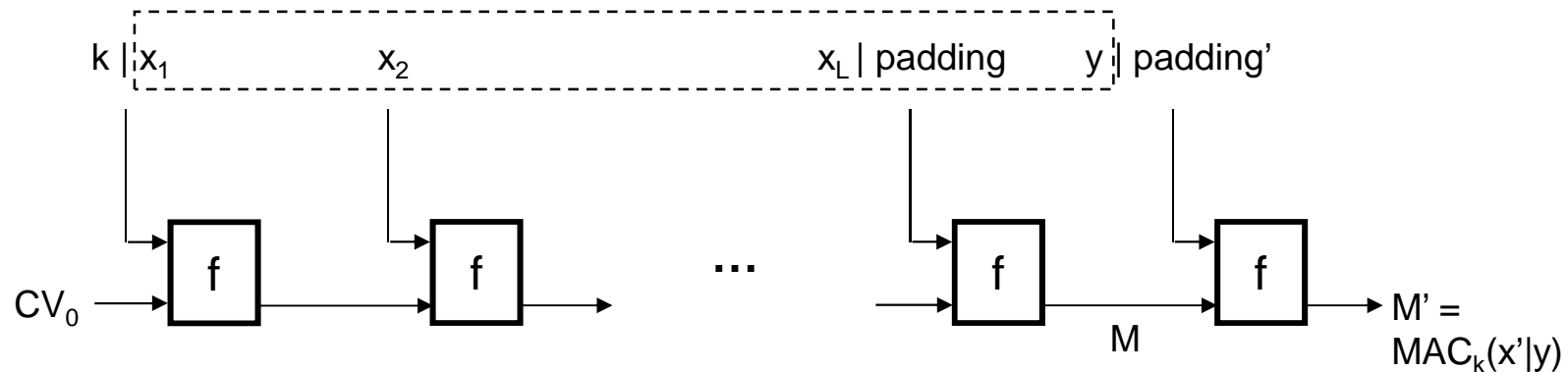
- message authentication
  - naïve constructions
  - HMAC
  - CBC-MAC
  - CMAC
- authenticated encryption
  - generic combinations
  - CCM
  - OCB
  - GCM



# Secret prefix method

$$\text{MAC}_k(x) = H(k|x)$$

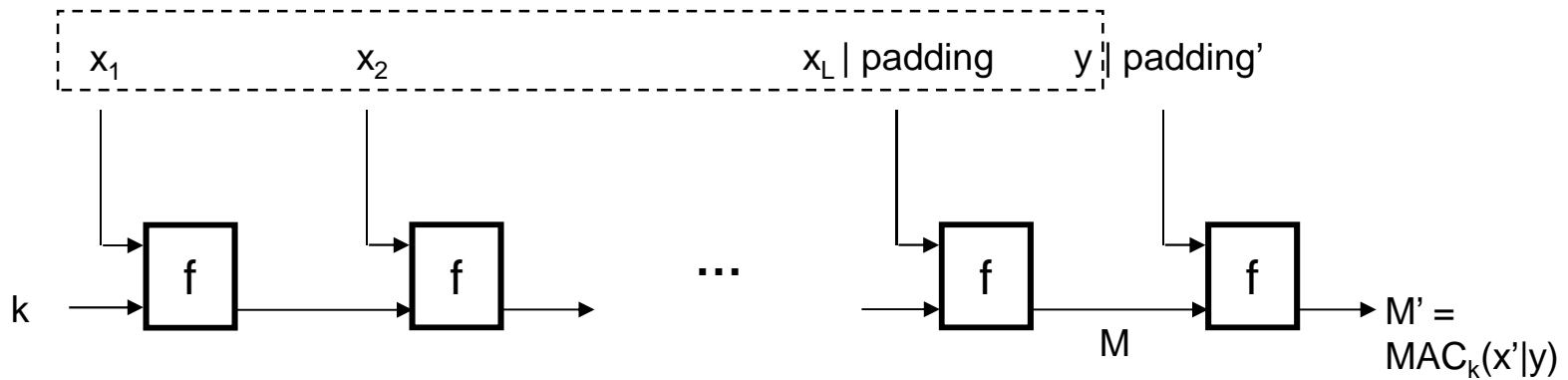
- insecure !
  - assume an attacker knows the MAC on  $x$ :  $M = H(k|x)$
  - he can produce the MAC on  $x'|y$  as  $M' = f(M,y)$ , where  $x'$  is  $x$  with padding and  $f$  is the compression function of  $H$



# A similar mistake

$$\text{MAC}_k(x) = H_k(x)$$

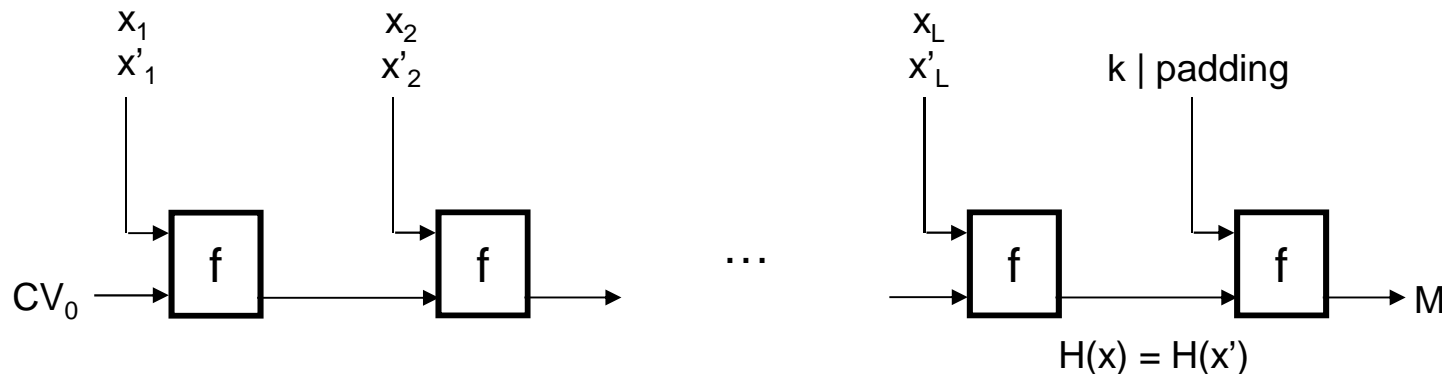
where  $H_k(\cdot)$  is  $H(\cdot)$  with  $\text{CV}_0 = k$

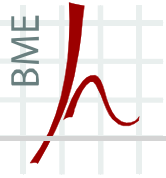


# Secret suffix method

$$\text{MAC}_k(x) = H(x|k)$$

- insecure if H is not collision resistant
  - using a birthday attack, the attacker finds two inputs  $x$  and  $x'$  such that  $H(x) = H(x')$  (can be done off-line without the knowledge of  $k$ )
  - then obtaining the MAC  $M$  on one of the inputs, say  $x$ , allows the attacker to forge a text-MAC pair  $(x', M)$
- weakness
  - key is involved only in the last step





# Envelop method

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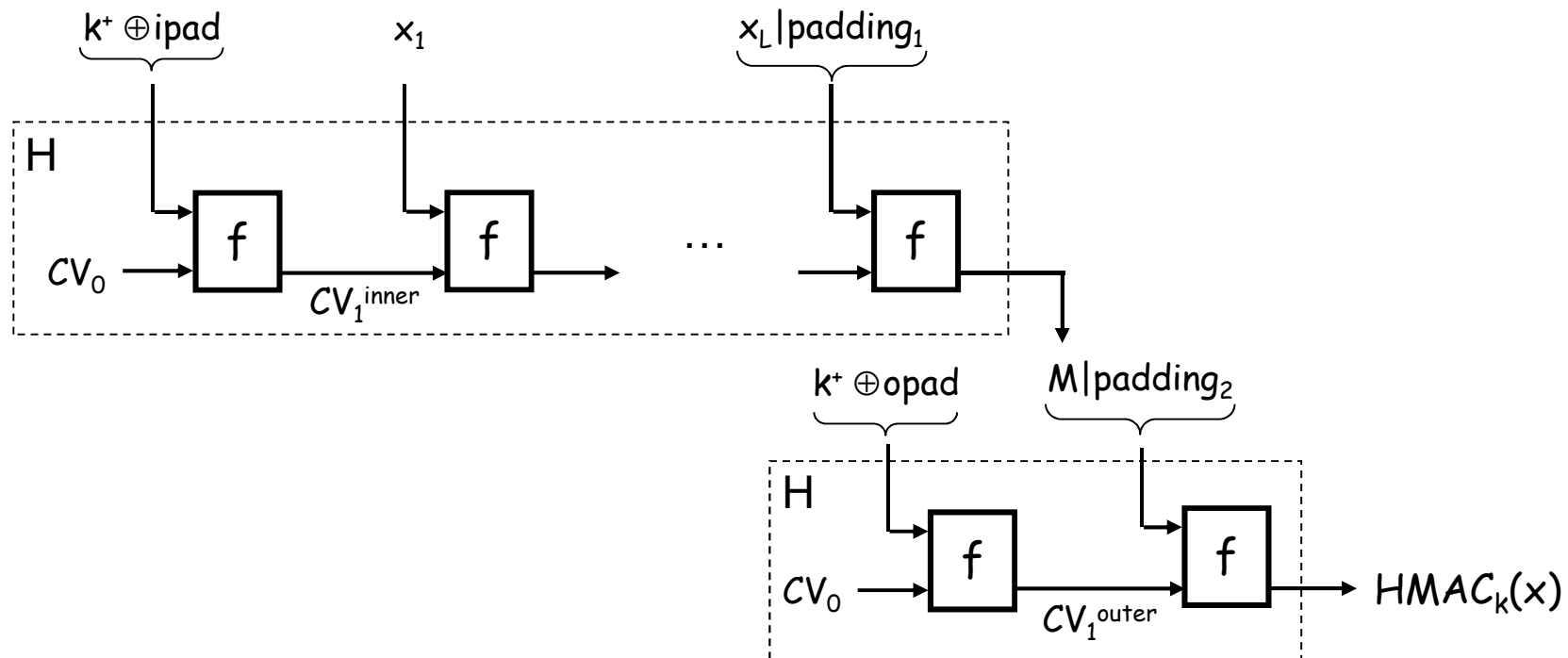
$$\text{MAC}_K(x) = H(k|x|k)$$

- a key recovery attack has been discovered on this scheme (requiring  $2^{64}$  text-MAC pairs for MD5 with 128-bit key)
- although, not really practical, the attack still represents an architectural flaw

$$\text{HMAC}_k(x) = H( (k^+ \oplus \text{opad}) \mid H( (k^+ \oplus \text{ipad}) \mid x ) )$$

where

- $h$  is a hash function with input block size  $b$  and output size  $n$
- $k^+$  is  $k$  padded with 0s to obtain a length of  $b$  bits
- $\text{ipad}$  is 00110110 repeated  $b/8$  times
- $\text{opad}$  is 01011100 repeated  $b/8$  times

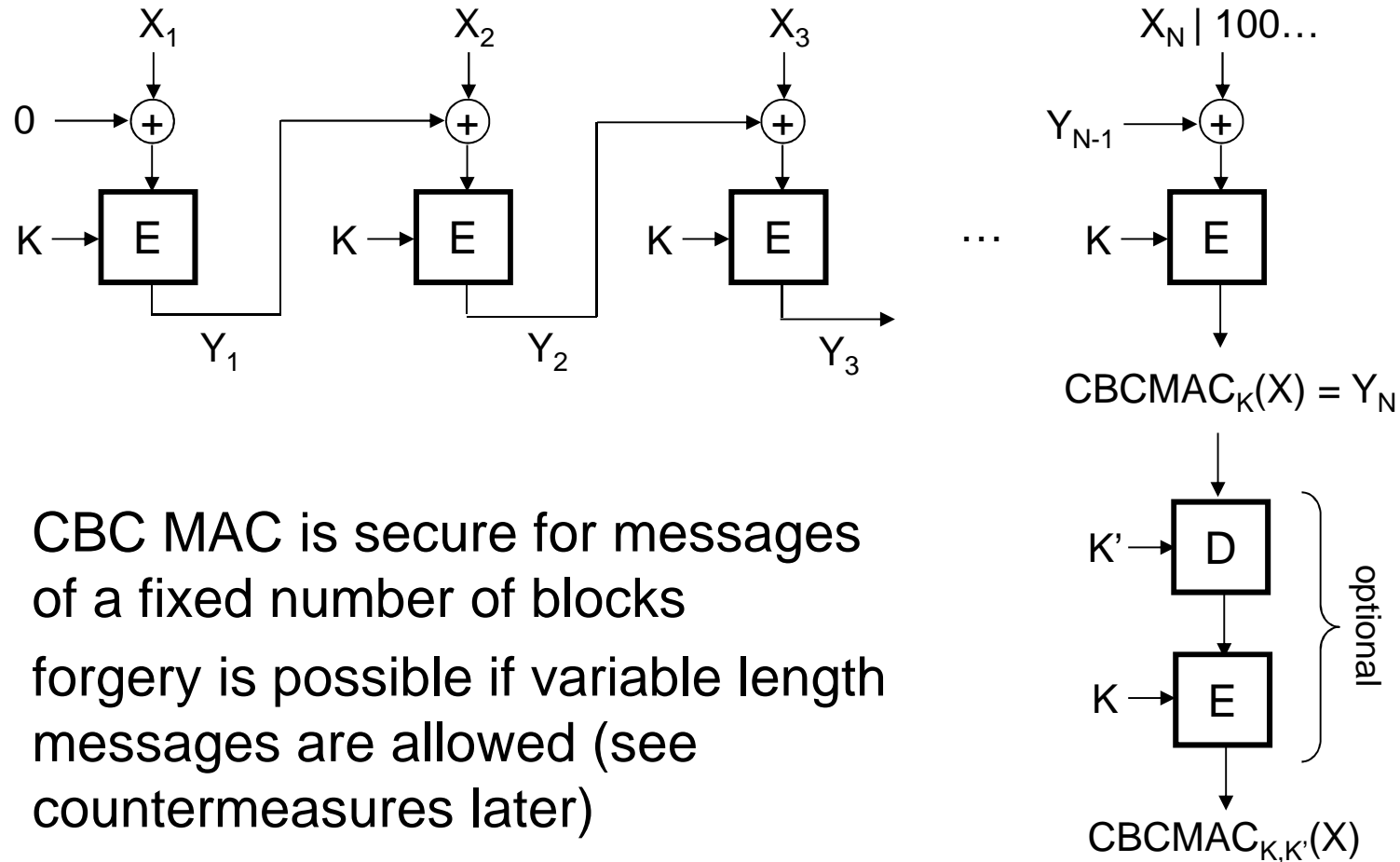


$$\text{MAC}_K(x) = E_K(H(x))$$

- off-line search for messages with colliding MAC values is possible here without the knowledge of k → H must be collision resistant !
- collision resistant hash functions usually have larger output size than the block size of the block cipher → which mode to use to encrypt the hash?
- two messages having the same hash value will have the same MAC value under all keys



# CBC-MAC

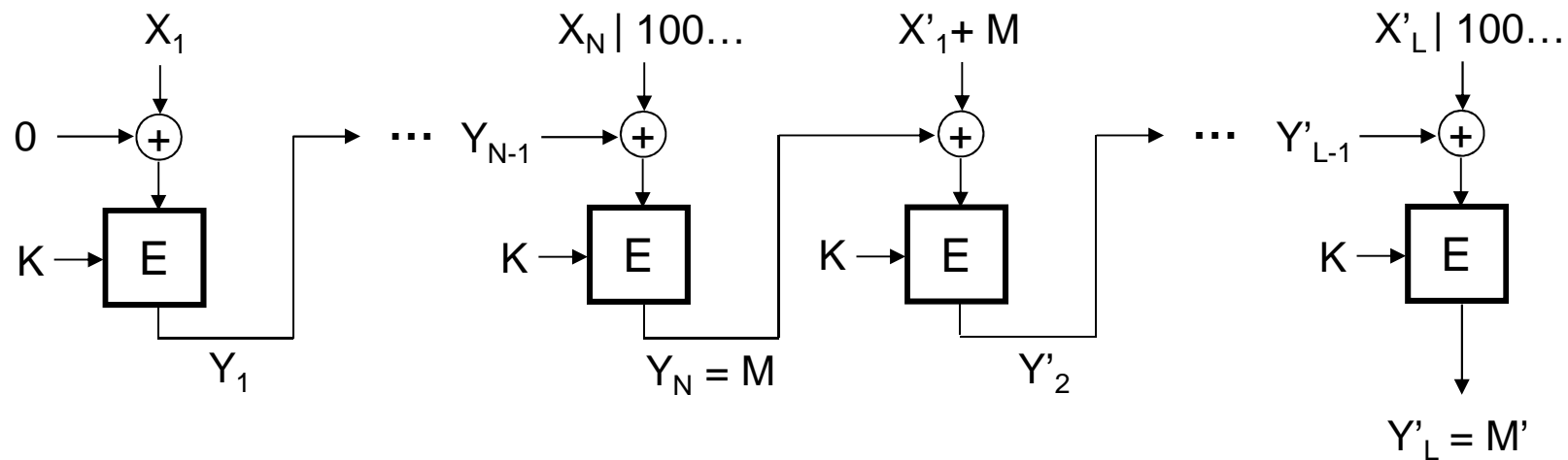


- CBC MAC is secure for messages of a fixed number of blocks
- forgery is possible if variable length messages are allowed (see countermeasures later)

# A known-text forgery

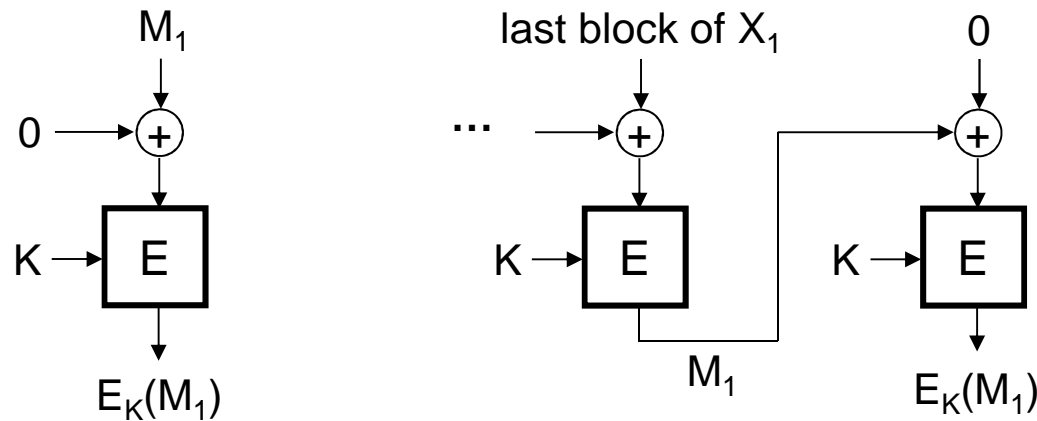
- given two text-MAC pairs  $(X, M)$  and  $(X', M')$ , a third valid text-MAC pair can be computed as follows:

$$(X \mid 100\dots \mid X'_1 + M \mid X'_2 \mid \dots \mid X'_L, M')$$



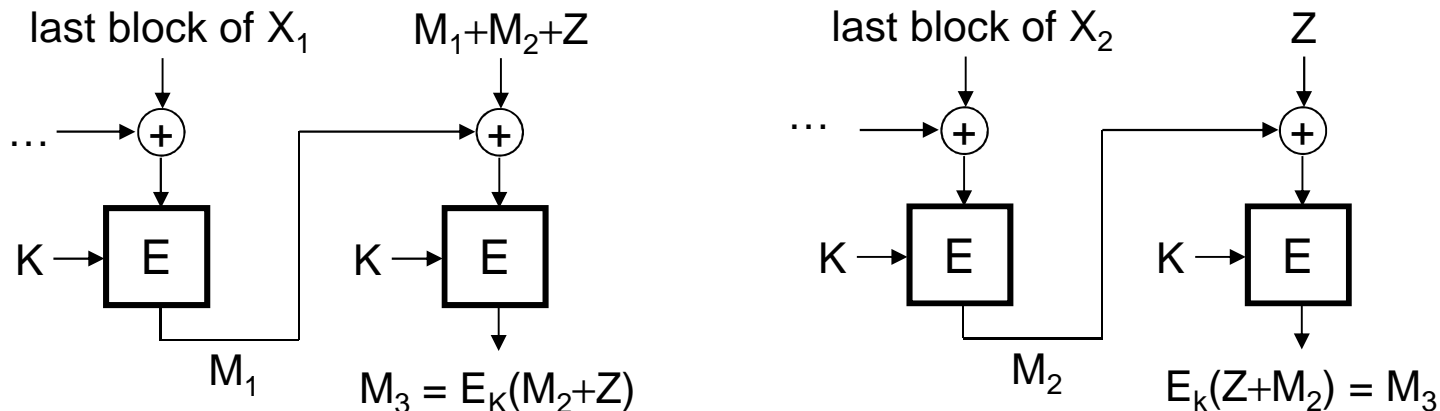
# A chosen-text forgery

- given a known text-MAC pair  $(X_1, M_1)$
- request MAC for  $M_1$ , receive  $M_2 = E_k(M_1 + 0) = E_k(M_1)$
- $M_2$  is the MAC of the message  $(X_1|0)$



# Another chosen-text forgery

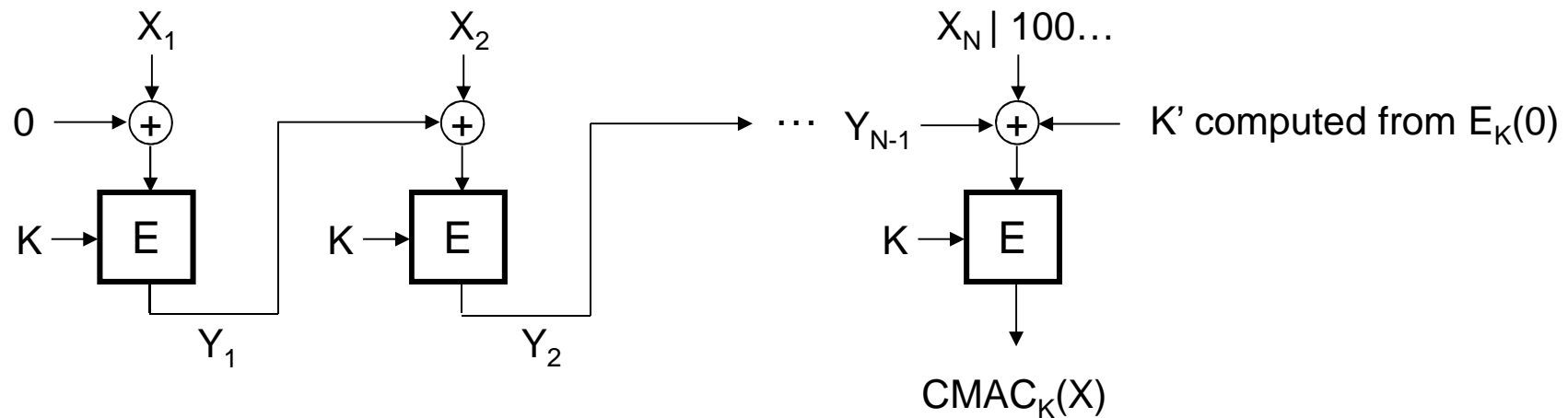
- given two known text-MAC pairs:  $(X_1, M_1)$ ,  $(X_2, M_2)$
- request a MAC for message  $X_1|M_1+M_2+Z$ , where  $Z$  is an arbitrary block
- receive  $M_3 = E_K(M_1+M_2+Z+M_1) = E_K(M_2 + Z)$
- $M_3$  is also the MAC for message  $X_2|Z$



# How to use CBC-MAC in practice?

- use the optional final encryption
  - reduces the threat of exhaustive key search (key is  $(K, K')$  → key length is doubled)
  - prevents the previously presented existential forgeries
  - has marginal overhead (only last block is encrypted multiple times)
- start the message with an extra block containing the length of the message
- use  $K$  to encrypt the length and obtain  $K' = E_K(\text{length})$ , and use  $K'$  as the MAC key (i.e., use message dependent MAC keys)

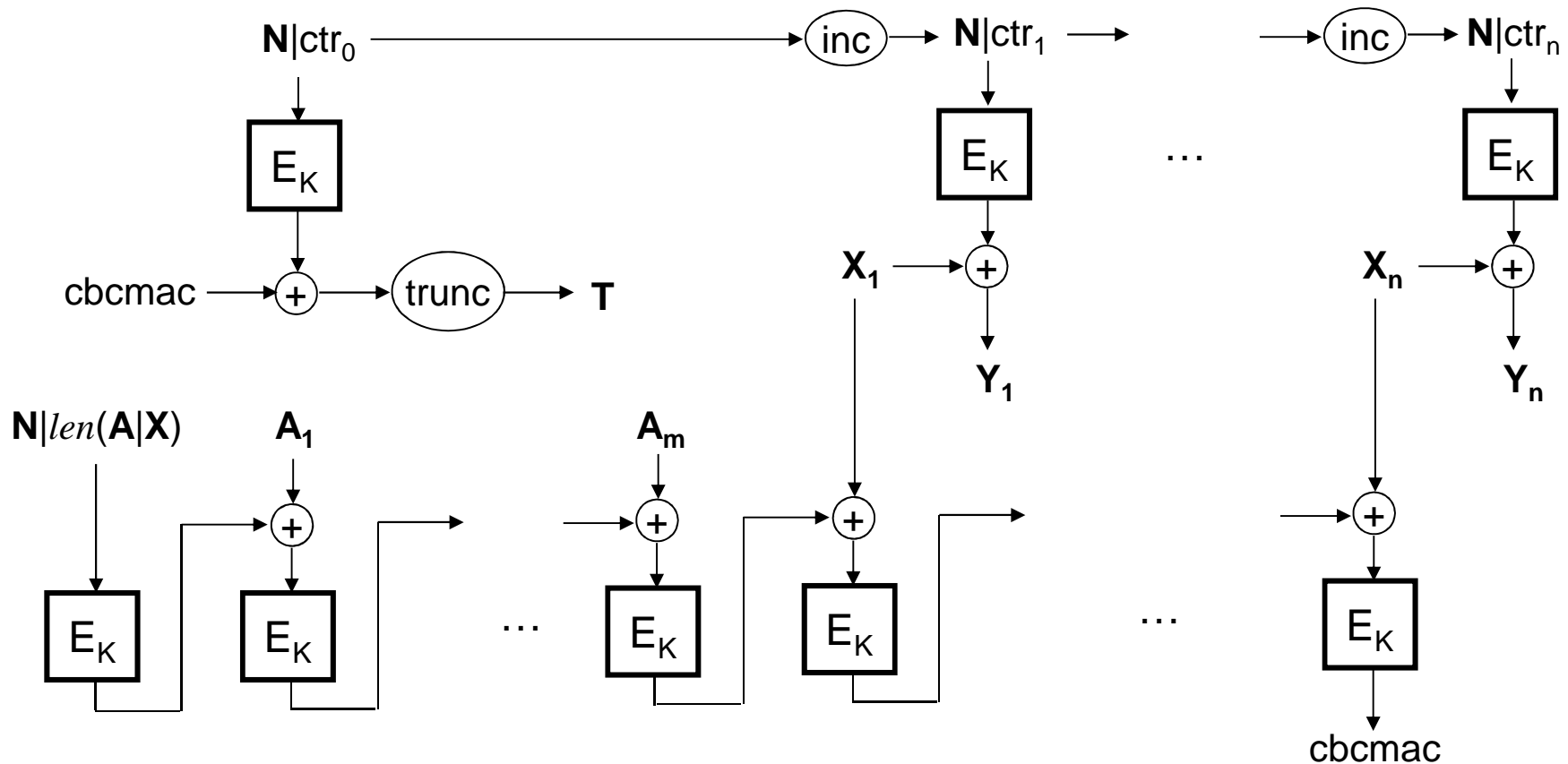
- proposed to fix problems with CBC-MAC



# Authenticated encryption schemes

- simultaneously protect the confidentiality and the integrity of a message
- motivations:
  - to prevent chosen-ciphertext attacks (such as the Vaudenay attack)
    - the decryption oracle immediately recognizes improperly constructed ciphertexts and refuses to decrypt them
    - attacker can construct a correct ciphertext only if he already knows the plaintext → decryption oracle becomes useless
  - efficiency (in some cases)
    - needs fewer operations if the message is encrypted and the authentication tag is computed in a single pass
- approaches:
  - specialized schemes (e.g., CCM, OCB, GCM)
  - generic combination of encryption and MAC (but be careful !)
    - $E_{K_1}(X|MAC_{K_2}(X))$  (check for padding oracle attack !)
    - $E_{K_1}(X)|MAC_{K_2}(X)$  (check for padding oracle attack !)
    - $E_{K_1}(X)|MAC_{K_2}(E_{K_1}(X))$  (considered to be the most secure approach)

# CCM – CTR mode with CBC-MAC

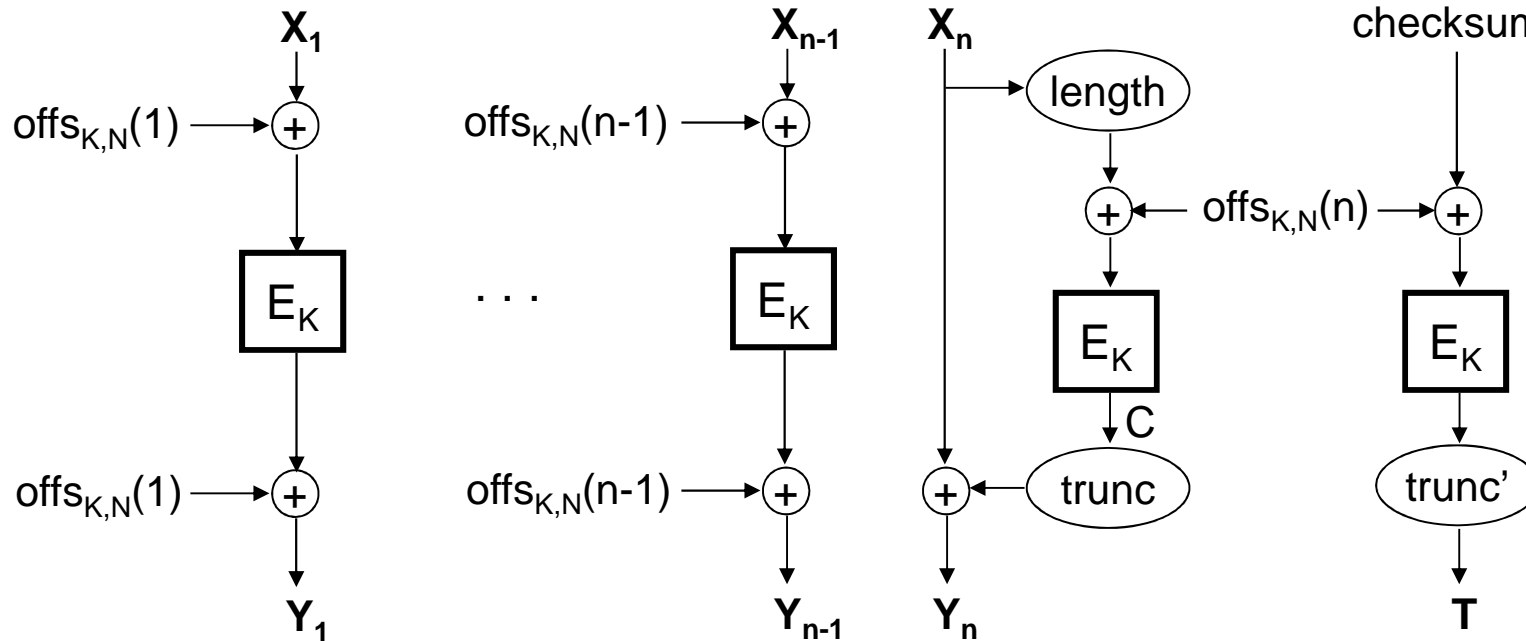


- input: message  $X$ , key  $K$ , associated data  $A$ , nonce  $N$
- output: encrypted message  $Y$ , authentication tag  $T$  (encrypted CBC MAC value)
- single key
- two passes ( $2n+m+2$  invocation of the block cipher)



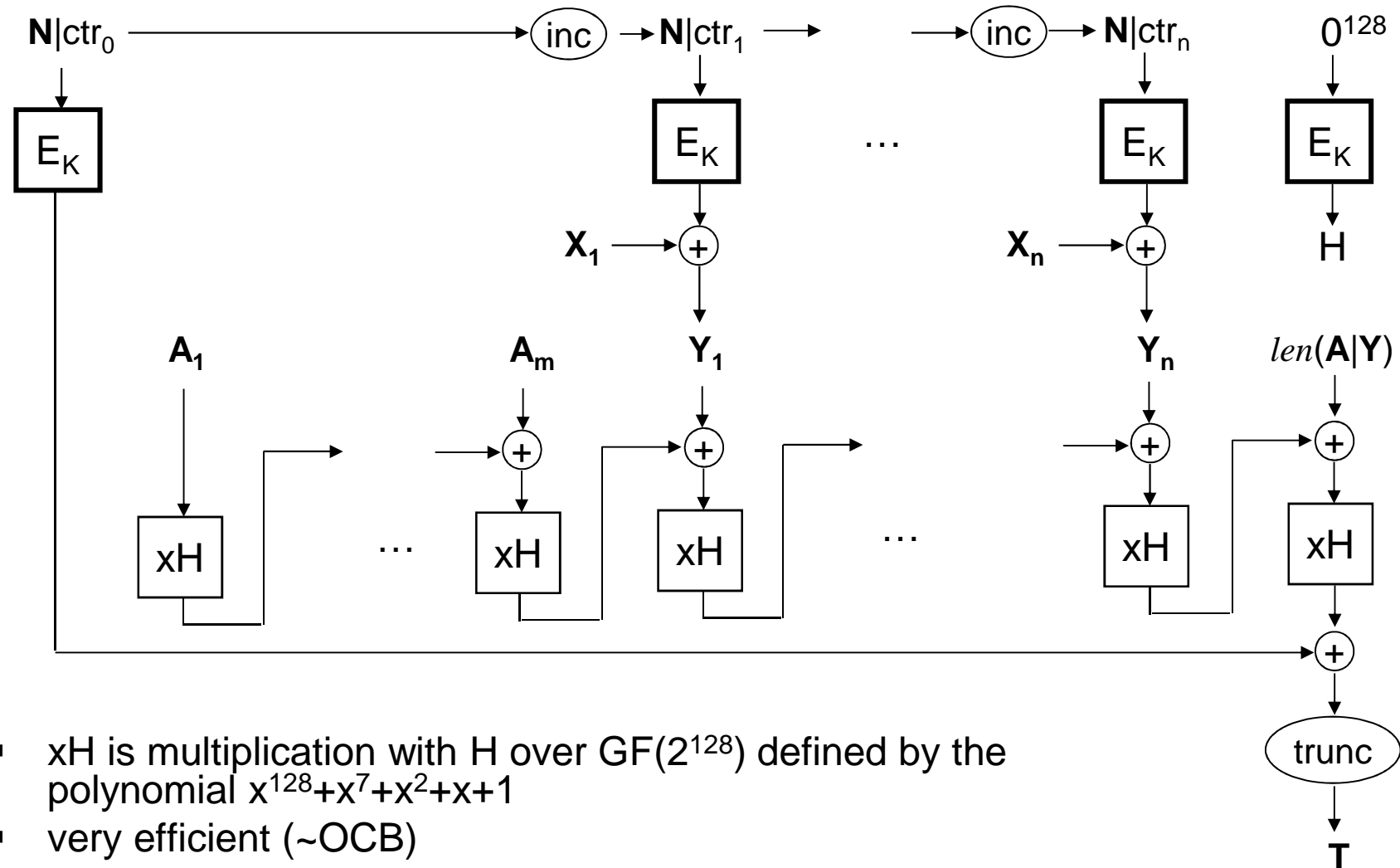
# OCB – Offset Code Book

$$\text{checksum} = X_1 \oplus \dots \oplus X_{n-1} \oplus Y_n \oplus C \oplus \text{checksum}$$



- single key, single pass
- no associated data
- preserves plaintext length
- provably secure
- patented

# GCM – Galois/Counter Mode



- $xH$  is multiplication with  $H$  over  $GF(2^{128})$  defined by the polynomial  $x^{128}+x^7+x^2+x+1$
- very efficient ( $\sim$ OCB)
- provably secure and not patented

- naïve hash based MAC constructions are usually not secure
- better to use standard, well-studied constructions, e.g., HMAC
- CBC-MAC
  - interesting, because it does not need a hash function, but it can use the same block cipher that is used for encryption, anyway
  - existential forgeries against CBC-MAC exist, but there are countermeasures (e.g., adding context data such as message length to the message, multiple encryption of the last block, etc.)
- be careful with generic constructions for authenticated encryption
- specific authenticated encryption modes have some advantages
  - efficiency: the two goals may be achieved in a single pass
  - security: no information is leaked through a padding oracle
- CCM
  - single key, two pass, associated data, not patented
- OCB
  - single key, single pass, no associated data, patented
- GCM
  - single key, single pass, associated data, not patented
  - performance is comparable to OCB