

Key establishment in ad hoc networks

exploiting
- physical contact;
- mobility and vicinity;

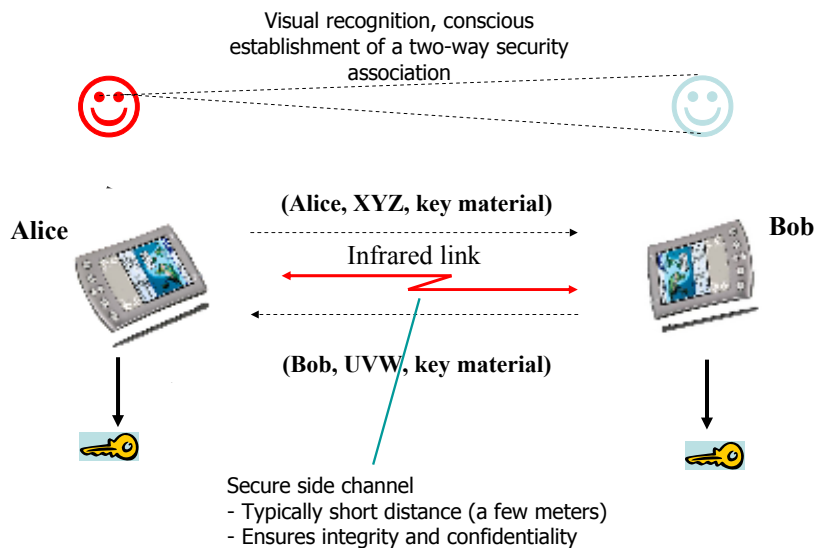
Exploiting physical contact

- target scenarios
 - modern home with multiple remotely controlled devices
 - DVD, VHS, HiFi, doors, air condition, lights, alarm, ...
 - modern hospital
 - mobile personal assistants and medical devices, such as thermometers, blood pressure meters, ...
- common in these scenarios
 - transient associations between devices
 - physical contact is possible for initialization purposes
- the **resurrecting duckling** security policy
 - at the beginning, each device has an empty *soul*
 - each empty device accepts the first device to which it is physically connected as its master (imprinting)
 - during the physical contact, a device key is established
 - the master uses the device key to execute commands on the device, including the *suicide* command
 - after suicide, the device returns to its empty state and it is ready to be imprinted again

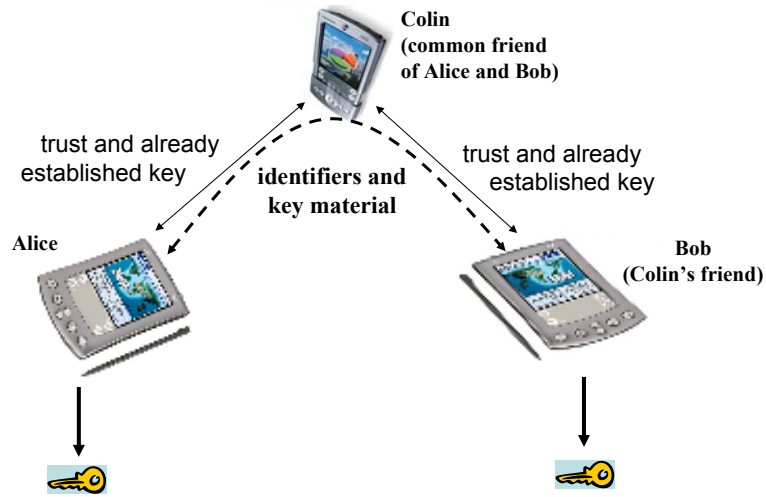
Does mobility increase or reduce security ?

- Mobility is usually perceived as a major security challenge in networking
 - Wireless communications
 - Sporadic availability of the user/node
 - Higher vulnerability of the device
 - Reduced computing capability of the devices
- However, in real life, people often move (and gather) to increase security
 - Face to face meetings
 - Transport of assets and documents
 - Authentication by physical presence
- Can we take advantage of mobility to increase security in networking?
- Yes, we can, assuming that
 - nodes are operated by humans
 - when in the vicinity of each other, nodes can use a **secure side channel** (e.g., infra red) to exchange a key
 - each node has some **friends** (peers that are trusted by the node), and there is already a key shared between each pair of friends

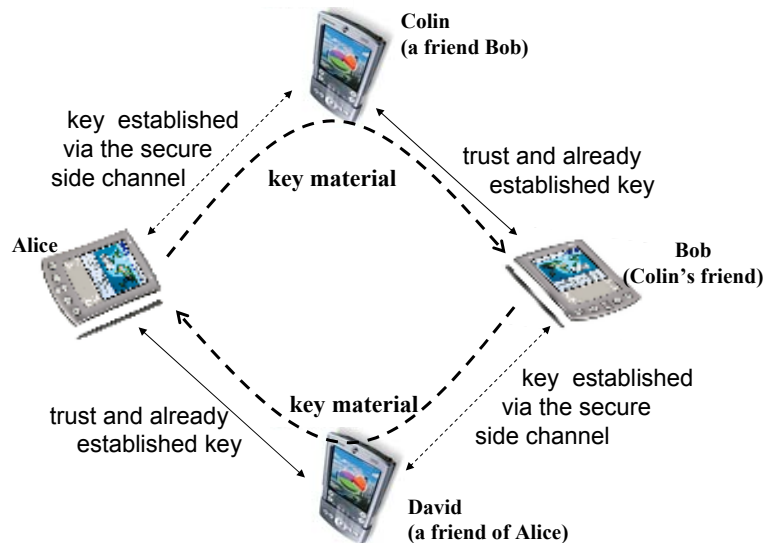
Exploiting vicinity and the secure side channel



Taking advantage of common friends



What if there's no common friend?



A possible implementation

```
msg1  $u \rightarrow v : f, r_u$ 
msg2  $v \rightarrow u : g, r_v$ 
msg3  $u \rightarrow g : u, \{d_{u \rightarrow g}, req, v, k_u, r_v\}k_{ug}$ 
msg4  $g \rightarrow v : g, \{d_{g \rightarrow v}, rep, u, k_u, r_v\}k_{vg}$ 
msg3'  $v \rightarrow f : v, \{d_{v \rightarrow f}, req, u, k_v, r_u\}k_{vf}$ 
msg4'  $f \rightarrow u : f, \{d_{f \rightarrow u}, rep, v, k_v, r_u\}k_{uf}$ 
 $u, v : k_{uv} = h(k_u, k_v)$ 
```

- notes:

- single trusted party is replaced with two parties trusted by one entity each
- if f and g are not colluding, then they cannot compute kuv
- both u and v trust at least one of f and g for not colluding

Pace of establishment of the security associations

- **Depends on several factors:**

- Area size
- Number of communication partners: s
- Number of nodes: n
- Number of friends
- Mobility model and its parameters (speed, pause times, ...)

Desired security associations :
 $p_{ij} = 1$, if i and j wants to setup
a shared key, and 0 otherwise

Established security associations :
 $e_{ij}(t) = 1$, if at time t nodes i and j
already share a key, and 0 otherwise

Convergence :
$$r(t) = \frac{\sum_{i,j} e_{ij}(t) \cdot p_{ij}}{\sum_{i,j} p_{ij}}$$

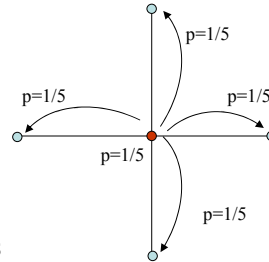
and the convergence time t_M is the earliest
time at which $r(t) = 1$.

Mobility models

- Random walk
 - discrete time
 - simple, symmetric random walk
 - **area:** Bounded and toroid grids (33x33, 100x100, 333x333)
 - **number of nodes:** 100

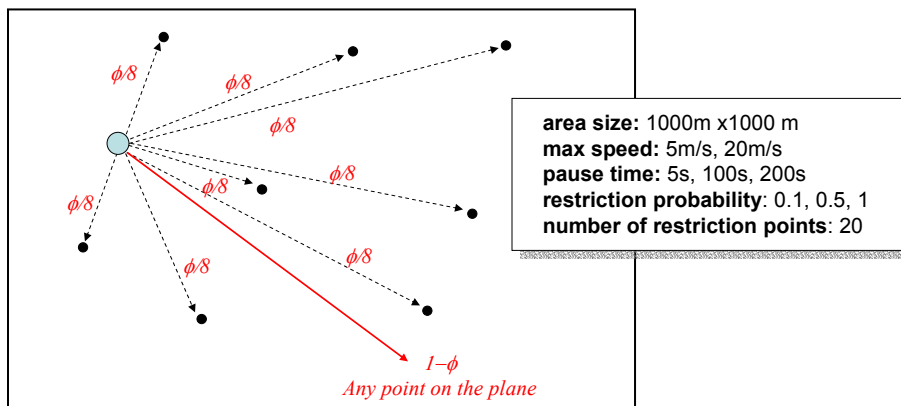
- Random waypoint
 - most commonly used in mobile ad hoc networks
 - continuous time
 - **area size:** 1000m x1000m
 - **max speed:** 5m/s, 20m/s
 - **pause time:** 5s, 100s, 200s
 - **security power range:** 5m (SSC), 50m 100m (radio)

- Common simulation settings
 - simulations are run 20 times
 - confidence interval: 95%

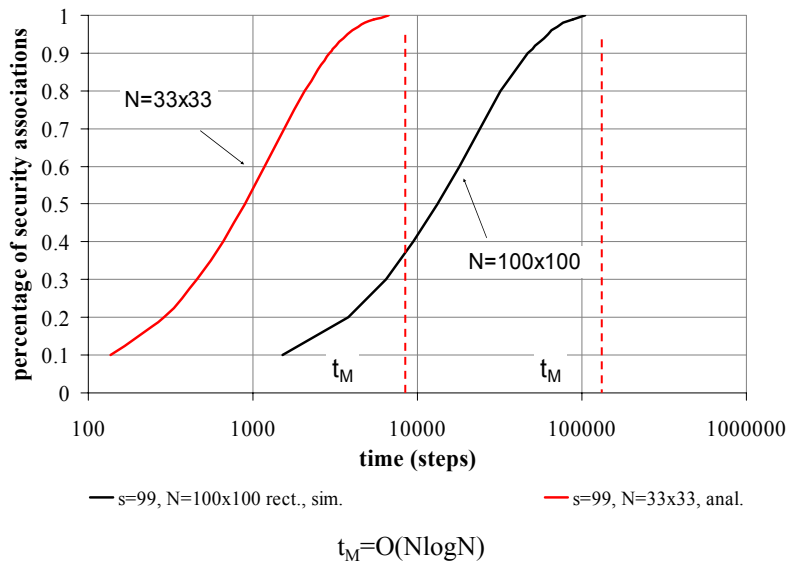


(Restricted) random waypoint

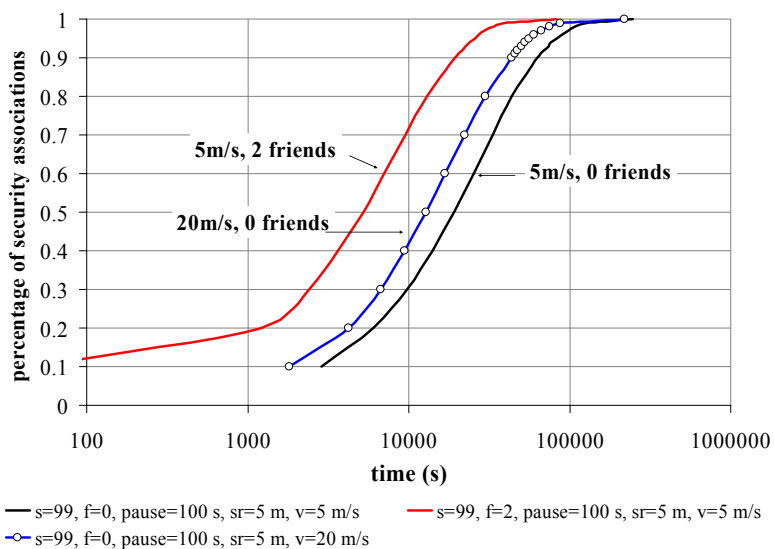
- Restricts the movement of nodes to a set of points with a predefined probability ϕ
- Regular random waypoint is a special case ($\phi = 0$)



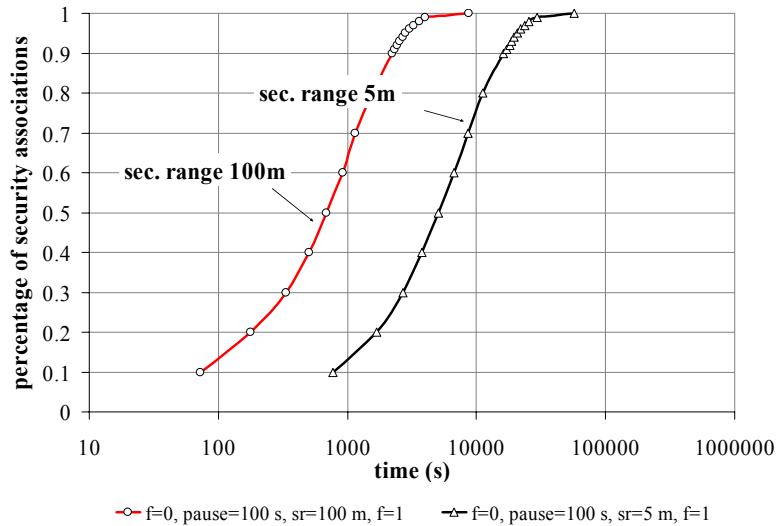
Size matters



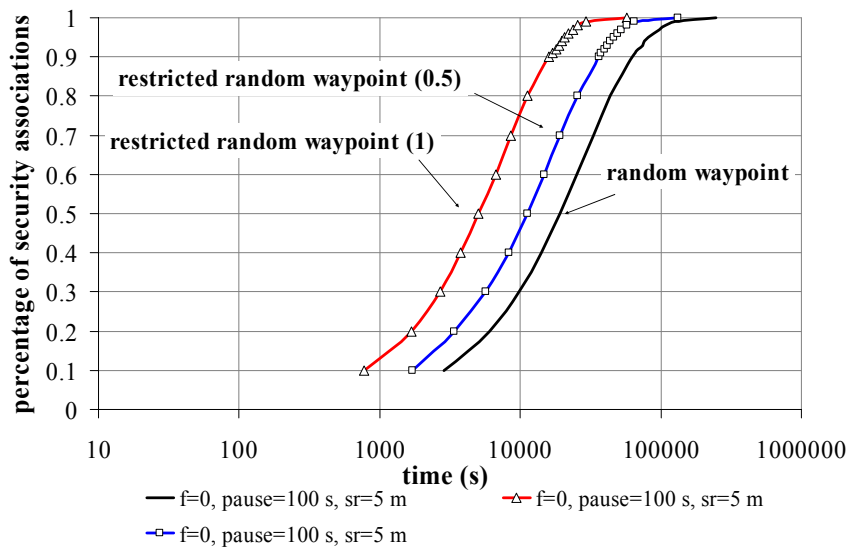
Friends help



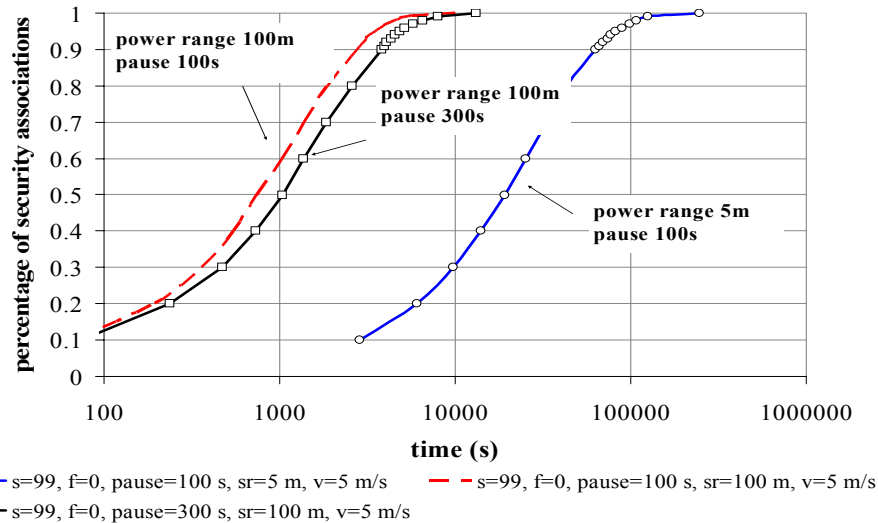
Security range matters



Meeting points help



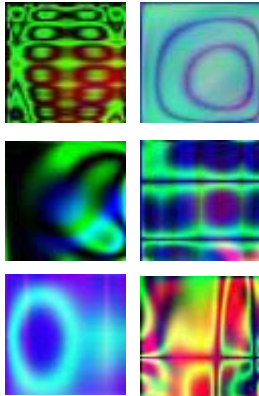
Pause time



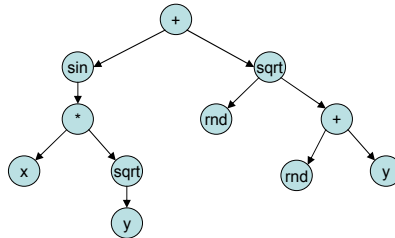
Can the secure side channel be based on radio?

- Diffie-Hellman with authentication of messages by the human operator of the devices
- Alice and Bob comes together
 - their devices execute the basic Diffie-Hellman protocol over the radio channel
 - Alice's device hashes the concatenation of all messages that it sent and that it received in the protocol
 - Bob's device hashes the concatenation of all messages that it received and that it sent in the protocol
 - the two hash must match
 - both devices display the hash values in some human readable format
 - select a set of words from a common dictionary based on the hash value
 - visualize the hash function with a Random Art image
 - the human operators compare the displayed hash value

Application of Random Art images



- the hash value is converted into three two-variable functions
 - each can be represented as a tree



- these formulae define the color value of each pixel of the resulting image

Can the secure side channel be based on radio?

→ Diffie-Hellman with I-codes

- special PHY layer that uses on-off keying (presence of signal means 1, absence of signal means 0)
- active adversary can turn a 0 into a 1, but not vice versa
- each message sent is encoded in such a way that it contains the same number of 0s and 1s (I-codes)
- messages cannot be modified in an unnoticeable way
- encoding messages with I-codes ensures the integrity of the communications → Man-in-the-Middle is excluded

Summary

- it is possible to establish pairwise shared keys in ad hoc networks without a globally trusted third party
- mobility, secure side channels, and friends are helpful
- the pace of establishment of the security associations is strongly influenced by the area size, the number of friends, and the speed of the nodes
- the proposed solution can easily be implemented with both symmetric and asymmetric crypto

Key establishment in sensor networks

key types;
establishment of link
keys using a short-term
master key;
random key pre-
distribution:
- the basic scheme, and
- some improvements;

Key establishment in sensor networks

- due to resource constraints, asymmetric key cryptography should be avoided in sensor networks
- we aim at setting up symmetric keys

- requirements for key establishment depend on
 - communication patterns to be supported
 - unicast
 - local broadcast
 - global broadcast
 - need for supporting in-network processing
 - need to allow passive participation

- useful key types
 - node keys – shared by a node and the base station
 - link keys – pairwise keys shared by neighbors
 - cluster keys – shared by a node and all its neighbors
 - network key – a key shared by all nodes and the base station

Setting up node, cluster, and network keys

- node key
 - can be preloaded into the node before deployment

- cluster key
 - can be generated by the node and sent to each neighbor individually protected by the link key shared with that neighbor

- network key
 - can also be preloaded in the nodes before deployment
 - needs to be refreshed from time to time (due to the possibility of node compromise)
 - neighbors of compromised nodes generate new cluster keys
 - the new cluster keys are distributed to the non-compromised neighbors
 - the base station generates a new network key
 - the new network key is distributed in a hop-by-hop manner protected with the cluster keys

Design constraints for link key establishment

- network lifetime
 - severe constraints on energy consumption
- hardware limits
 - 8-bit CPU, small memory
 - large integer arithmetics are infeasible
- no tamper resistance
 - nodes can be compromised
 - secrets can be leaked
- no a priori knowledge of post-deployment topology
 - it is not known a priori who will be neighbors
- gradual deployment
 - need to add new sensors after deployment

Traditional approaches

- use of public key crypto (e.g., Diffie-Hellman)
 - limited computational and energy resources of sensors
- use of a trusted key distribution server (Kerberos-like)
 - base station could play the role of the server
 - requires routing of key establishment messages to and from the base station
 - routing may already need link keys
 - unequal communication load on the sensors
 - base station becomes single point of failure
- pre-loaded link keys in sensors
 - post-deployment topology is unknown
 - single “mission key” approach
 - vulnerable to single node compromise
 - $n-1$ keys in each of the n sensors
 - excessive memory requirements
 - gradual deployment is difficult
 - doesn't scale

Link key setup using a short-term master key (LEAP)

- main assumptions:
 - any sensor node deployed will not be compromised within T_{\min} time
 - any node can discover its neighbors and set up neighbor relationships within $T_{\text{est}} < T_{\min}$ time
 - typically, T_{est} is a few seconds, so these assumptions make sense in practice
- protocol:
 - key pre-distribution phase
 - neighbor discovery phase
 - link key establishment phase
 - key erasure phase

Link key setup using a short-term master key (LEAP)

- key pre-distribution phase
 - before deployment, each node is loaded with K_l
 - each node u derives a node key K_u as $K_u = f(K_l, u)$, where f is a one-way function
- neighbor discovery phase
 - when a node deployed, it tries to discover its neighbors by broadcasting a HELLO message
$$u \rightarrow *: u, N_u$$
where N_u is a random nonce
 - each neighbor v replies with
$$v \rightarrow u: v, \text{mac}(K_v, v|N_u)$$
 - u can compute $f(K_l, v) = K_v$, and verify the authenticity of the reply

Link key setup using a short-term master key (LEAP)

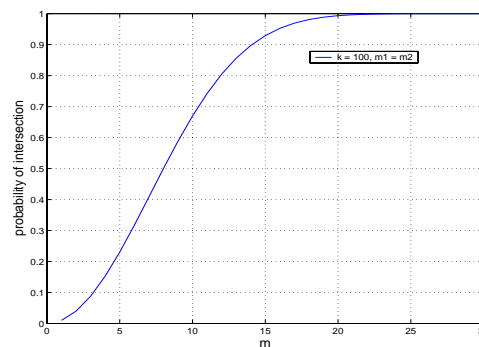
- link key establishment phase
 - u computes the link key $K_{uv} = f(K_v, u)$
 - v computes the same key
 - no messages are exchanged
 - note:
 - u does not authenticate itself to v, but ...
 - only a node that knows K_1 can compute K_{uv}
 - a compromised node that tries to impersonate u cannot know K_1 (see below)
- key erasure phase
 - T_{\min} time after its deployment, each node deletes K_1 and all keys it computed in the neighbor discovery phase

Random key pre-distribution – Preliminaries

Given a set S of k elements, we randomly choose two subsets S_1 and S_2 of m_1 and m_2 elements, respectively, from S .

The probability of $S_1 \cap S_2 \neq \emptyset$ is

$$\Pr\{S_1 \cap S_2 \neq \emptyset\} = 1 - \frac{(k - m_1)!(k - m_2)!}{k!(k - m_1 - m_2)!}$$



The basic random key pre-distribution scheme

- initialization phase
 - a large pool S of unique keys are picked at random
 - for each node, m keys are selected randomly from S and pre-loaded in the node (key ring)
- direct key establishment phase
 - after deployment, each node finds out with which of its neighbors it shares a key (e.g., each node may broadcast the list of its key IDs)
 - two nodes that discover that they share a key verify that they both actually possess the key (e.g., execute a challenge-response protocol)
- path key establishment phase
 - neighboring nodes that do not have a common key in their key rings establish a shared key through a path of intermediaries
 - each link of the path is secured in the direct key establishment phase

Setting the parameters

- connectivity of the graph resulting after the direct key establishment phase is crucial
- a result from random graph theory [Erdős-Rényi]:
 - in order for a random graph to be connected with probability c (e.g., $c = 0.9999$), the expected degree d of the vertices should be:

$$d = \frac{n-1}{n}(\ln(n) - \ln(-\ln(c))) \quad (1)$$

- in our case, $d = pn'$ (2), where p is the probability that two nodes have a common key in their key rings, and n' is the expected number of neighbors (for a given deployment density)
- p depends on the size k of the pool and the size m of the key ring

$$p = 1 - \frac{((k-m)!)^2}{k!(k-2m)!} \quad (3)$$

- $c \xrightarrow{(1)} d \xrightarrow{(2)} p \xrightarrow{(3)} k, m$

Setting the parameters – an example

- number of nodes: $n = 10000$
- expected number of neighbors: $n' = 40$
- required probability of connectivity after direct key establishment: $c = 0.9999$
- using (1):
 - required node degree after direct key establishment: $d = 18.42$
- using (2):
 - required probability of sharing a key: $p = 0.46$
- using (3):
 - appropriate key pool and key ring sizes:
 - $k = 100000, m = 250$
 - $k = 10000, m = 75$
 - ...

Qualitative analysis

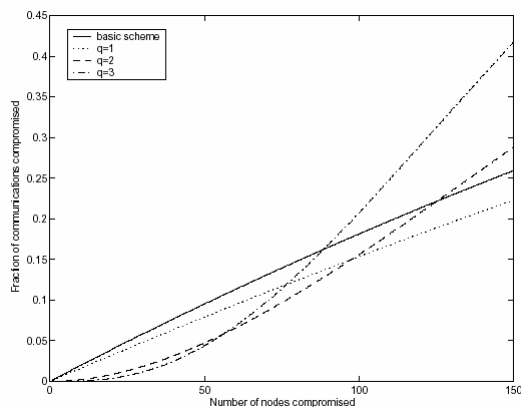
- advantages:
 - parameters can be adopted to special requirements
 - no need for intensive computation
 - path key establishment have some overhead ...
 - decryption and re-encryption at intermediate nodes
 - communication overhead
 - but simulation results show that paths are not very long (2-3 hops)
 - no assumption on topology
 - easy addition of new nodes
- disadvantages:
 - node capture affects the security of non-captured nodes too
 - if a node is captured, then its keys are compromised
 - these keys may be used by other nodes too
 - if a path key is established through captured nodes, then the path key is compromised
 - no authentication is provided

Improvements: q -composite rand key pre-distribution

- basic idea:
 - two nodes can set up a shared key if they have at least q common keys in their key rings
 - the pairwise key is computed as the hash of all common keys
- advantage:
 - in order to compromise a link key, all keys that have been hashed together must be compromised
- disadvantage:
 - probability of being able to establish a shared key directly is smaller (it is less likely to have q common keys, than to have one)
 - key ring size should be increased (but: memory constraints) or key pool size should be decreased (but: effect of captured nodes)

q -composite scheme: Simulation results

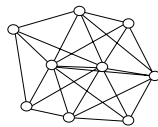
$$m = 200, p = 0.33$$



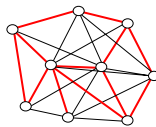
taken from: H. Chan and A. Perrig and D. Song, "Random key predistribution schemes for sensor networks", IEEE Security and Privacy Symp. (Oakland), 2003

Improvements: Multipath key reinforcement

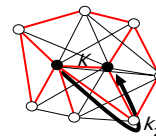
- basic idea:
 - establish link keys through multiple disjoint paths
 - assume two nodes have a common key K in their key rings
 - one of the nodes sends key shares k_1, \dots, k_j to the other through j disjoint paths
 - the key shares are protected during transit by keys that have been discovered in the direct key establishment phase
 - the link key is computed as $K + k_1 + \dots + k_j$



radio connectivity



shared key connectivity



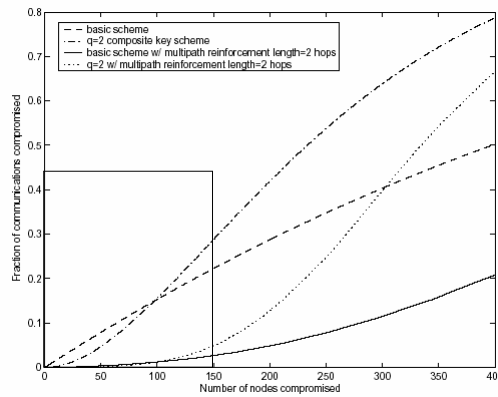
multipath key reinforcement

Improvements: Multipath key reinforcement

- advantages:
 - in order to compromise a link key, at least one link on each path must be compromised → increased resilience to node capture
- disadvantages:
 - increased overhead
- note:
 - multipath key reinforcement can be used for path key setup too

Multipath scheme: Simulation results

$m = 200, p = 0.33$



taken from: H. Chan and A. Perrig and D. Song, "Random key predistribution schemes for sensor networks", IEEE Security and Privacy Symp. (Oakland), 2003

Polynomial based key pre-distribution

- let f be a bivariate t -degree polynomial over a finite field $GF(q)$, where q is a large prime number, such that $f(x, y) = f(y, x)$

$$f(x, y) = \sum_{i,j=0}^t a_{ij}x^i y^j$$

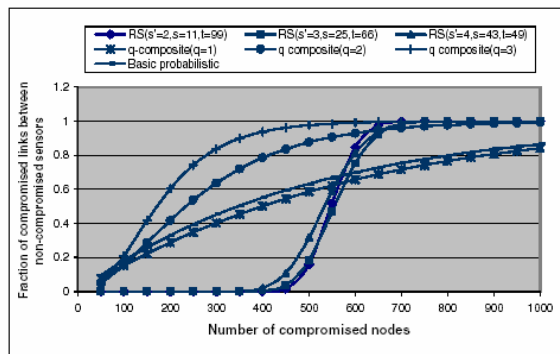
- each node is pre-loaded with a polynomial share $f(i, y)$, where i is the ID of the node
- any two nodes i and j can compute a shared key by
 - i evaluating $f(i, y)$ at point j and obtaining $f(i, j)$, and
 - j evaluating $f(j, y)$ at point i and obtaining $f(j, i) = f(i, j)$
- this scheme is unconditionally secure and t -collusion resistant
 - any coalition of at most t compromised nodes knows nothing about the shared keys computed by any pair of non-compromised nodes
- any pair of nodes can establish a shared key without communication overhead (if they know each other's ID)
- memory requirement of the nodes is $(t + 1) \log(q)$
- problem: t is limited by the memory constraints of the sensors

Polynomial based random key pre-distribution

- operation:
 - let S be a pool of bivariate t -degree polynomials
 - for each node i , we pick a subset of m polynomials from the pool
 - we pre-load into node i the polynomial shares of these m polynomials computed at point i
 - two nodes that have polynomial shares of the same polynomial f can establish a shared key $f(i, j)$
 - if two nodes have no common polynomials, they can establish a shared key through a path of intermediaries
- advantage:
 - can tolerate the capture of much more than t nodes (t can be smaller, but each node needs to store m polynomials)
 - in order to compromise a polynomial, the adversary needs to obtain $t + 1$ shares of that polynomial
 - it is very unlikely that $t + 1$ randomly captured nodes have all selected the same polynomial from the pool

Simulation results

- $m = 200, p = 0.33$



taken from D. Liu and P. Ning, "Establishing pairwise keys in distributed sensor networks", ACM CCS, 2003.

Matrix based key pre-distribution (Blom's scheme)

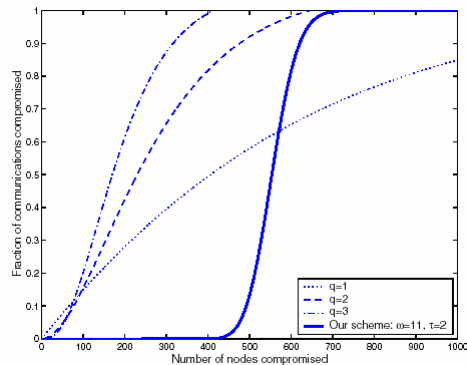
- let G be a $(t + 1) \times n$ matrix over a finite field $GF(q)$ (where n is the size of the network)
- let D be a random $(t + 1) \times (t + 1)$ symmetric matrix over $GF(q)$
- G is public, D is secret
- let $A = (DG)^T$ and $K = AG$
 - K is a symmetric matrix, because
$$K = AG = (DG)^T G = G^T D^T G = G^T D G = G^T A^T = (AG)^T = K^T$$
- each node i stores the i -th row of A
- any two nodes i and j can compute a shared key K_{ij}
 - i computes $A(i,.)G(.,j) = K_{ij}$
 - j computes $A(j,.)G(.,i) = K_{ji} = K_{ij}$

Matrix based random key pre-distribution

- G is as before
- D_1, \dots, D_k are random $(t + 1) \times (t + 1)$ symmetric matrices
- $A_v = (D_v G)^T$ and $\{A_v\}$ is the pool (of spaces)
- for each node i , we pick a random subset of the pool and pre-load in the node the i -th row of the selected matrices (i.e., $A_v(i,.)$ for each selected v)
- if two nodes i and j both selected a common matrix A_v , then they can compute a shared key using Blom's scheme
- if two nodes don't have a common space, they can setup a key through intermediaries

Simulation results

$m = 200, \rho = 0.33$



taken from W. Du and J. Deng and Y. S. Han and P. K. Varshney, "A pairwise key pre-distribution scheme for wireless sensor networks", ACM CCS, 2003

Assumptions revisited (and more) [DiPietro et al.]

- the connectivity graph resulting after the first phase of the basic protocol is not a random graph (in the sense of Erdős-Rényi)
 - an edge between two nodes exists if they have at least one common key AND they are in power range of each other
 - the Erdős-Rényi theorem may not hold for these types of graphs
- almost sure connectivity after the first phase of the basic protocol is ensured if
 - $m^2 / k = c \log(n) / n$
 - $k > n-1$
 - $m > 4$

Assumptions revisited (and more) [DiPietro et al.]

- a definition of security:
 - a network is *redoubtable*, if the probability that compromising a sub-linear fraction of nodes (uniformly chosen at random) can compromise a constant fraction of links in the network is 0
- a network is redoubtable if $m/k \sim 1/n$
- a practical choice of parameters:
 - $m = \log(n)$
 - $k = n \log(n)$

Summary

- in sensor networks, we need different types of keys
- node keys, cluster keys, and network keys can be established relatively easily using the technique of key pre-loading and using already established link keys
- link keys can be established using a short-term master key or with the technique of random key pre-distribution