

Risk analysis lab 11 2019. 12. 10. (Modern Portfolio Theory 2)

1. Load the supplied data from `s.csv`, containing daily returns for N asset and T days. Calculate its mean vector as $\mathbf{m} = \{E(s_1), E(s_2), \dots, E(s_N)\}$, and its covariance matrix Σ .
2. Generate a random portfolio vector $\mathbf{w} = \{w_1, w_2, \dots, w_N\}$ and $-1 < w_i < 1$ (short selling is allowed). Scale the portfolio to reach a profit of 0.1.

If we define $x(t) = \sum_{i=1}^N w_i s_i(t)$, then $x \sim N(\mu, \sigma)$ (CLT), where $\mu = \mathbf{w}^T \mathbf{m}$ and $\sigma^2 = \mathbf{w}^T \Sigma \mathbf{w}$.

Display the variance of the given portfolio.

3. Determine the optimal portfolio to minimize the risk:

$$\mathbf{w}_{opt} = \underset{\mathbf{w} : \mathbf{w}^T \boldsymbol{\mu} = b}{\operatorname{argmin}} \mathbf{w}^T \Sigma \mathbf{w}$$

The optimal portfolio can be calculated as a quadratic optimization problem. Use `scipy minimize` to obtain the optimal portfolio:

<https://docs.scipy.org/doc/scipy/reference/tutorial/optimize.html>

Display the variance of the given portfolio for $b=0.1$.