

Risk analysis lab 8 2019. 11. 05. (Sampling methods II.)

- 1) Write a function to generate random vectors (\mathbf{y}) in the N dimensional binary space according to the following distribution:

$$P(\mathbf{y}) = \prod_{i=1}^N p_i^{y_i} (1-p_i)^{1-y_i}$$

$$\mathbf{y} \in \{0,1\}^N, P(y_i = 1) = p_i, P(y_i = 0) = 1 - p_i$$

e.g.:

```
def generateY(p, N):  
    ...  
    return y
```

- 2) Write a function to estimate the risk using basic Monte Carlo sampling ([Risk Analysis lecture slides 57](#)):

$$\text{risk} = P(\mathbf{y}^T \mathbf{h} > C) \approx \frac{1}{K} \sum_{\mathbf{y}^T \mathbf{h} > C} 1$$

To generate the samples, use `generateY` function.

e.g.:

```
def calcMC(p, h, K):  
    ...  
    return risk
```

- 3) Try the algorithm for different K ($K = 10$, $K = 100$ and $K = 1000$), then compare the mean squared error (between the real and the estimated risk) and the running times of the estimation. As a benchmark, use the Brute-force algorithm.

Hint: [Measuring execution time](#)

As before, to test the program generate an example \mathbf{h} and \mathbf{p} , with $N=17$.