Convergence of the Key Algorithm of Traffic-Flow Analysis

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The traffic-flow analysis (TFA) [1] is a novel method for the performance estimation of communication systems. TFA is a combination of simulation and numerical methods. In the first step, TFA distributes the traffic in units of properly chosen size using the actual routing algorithm of the network. In the second step, TFA adjusts the time distribution of the traffic according to the finite capacities of the network. The convergence of the algorithm used in the second step of TFA is proven in this paper. The speed of convergence is also examined.

1. Introduction

The traffic-flow analysis (TFA) is a simulation-like method for the fast performance estimation of communication systems. The method can be used with any traffic model that satisfies the criteria published in [1].

Unlike discrete-event simulation, TFA does not model the travel of each packet through the network individually. It uses statistics to model the network load of applications. The method distributes traffic (the statistics) in the network first, and calculates the specific traffic conditions for each line and switching node later. This calculation requires an algorithm for the appropriate addition of the statistics considering also the finite capacities of each line and node in the network. The algorithm depends on the selected traffic model (the type of statistics). Using the throughput distribution as the traffic model, a two step algorithm was proposed in the original paper. In the first step, convolution is used to sum up all the throughput distribution statistics that were carried through a given network element (line or node). However, this summation may result in statistics that would contradict with the finite capacity of the

given element. (E.g.: with a non-zero probability, higher throughput than the line capacity could occur.) For this reason, in the second step, an iterative method is applied to correct the statistics according to the finite capacity of that element. This method seemed to work fine, but its convergence was not examined in [1]. The recent paper presents a formal proof for the convergence of the method. Also, the convergence speed and stopping criteria of the algorithm are also determined so that the method can be used in a network expert system like ImiNet [2].

The paper is organized as follows: first, the problem is formalized; second, by means of a series of theorems, the convergence of the questioned algorithm is proven; finally the convergence speed is examined.

2. The Formalization of the Problem

The parallel reading of Section 3.3 of the original paper proposing TFA [1] may help the reader to understand the role of the algorithm, but it is not necessary.
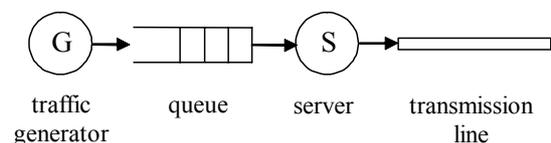
Let us consider the following block diagram.

Figure 1. The elements of the network

The task of the server is to transfer the bitstream of the traffic generator through the transmission line of capacity K bits per second. We shall formalize the problem as follows.

Let the random variable ξ denote the **length of the bitstream produced** for a period of T by generator G. Let m denote the expected value of ξ: $\mathbb{E}(\xi)=m$, and let σ denote the standard deviation of ξ: $\mathbb{D}(\xi)=\sigma$. This

bitstream is to be transferred through a line that can transfer K bits in a T time interval. Assuming that $\xi_1, \xi_2, \ldots \xi_n$ are independent and follow the same distribution during the consecutive $T_1, T_2, \ldots T_n$ time intervals (where $T_1 = T_2 = \ldots = T_n = T$). Let p_k denote the probability of the event that generator G produces a bitstream of length k in T time: $\mathbb{P}(\xi=k)=p_k$ (It was denoted by $p_T[k]$ in [1].) Of course, ξ is a non-negative discrete random variable, which can only take natural numbers as its values: $\xi \in \mathbb{N}$.

Let $\zeta^{(n)}$ denote the ***number of bits to be transferred*** in T_n (the n-th time slot) through a line of capacity K bits per second. $\mathbb{P}(\zeta^{(n)}=k)= p_k^{(n)}$. These bits may be newly arrived ones or may have arrived earlier and are still waiting in the queue.

The following recursive formula gives the probability of the event that the number of bits to be transferred in the n-th time-slot is exactly k:

$$p_k^{(n)} = p_k \sum_{l=0}^{K} p_l^{(n-1)} + \sum_{l=1}^{k} p_{l+K}^{(n-1)} p_{k-l} \quad for \; \forall k,$$
$$where \; p_k^{(0)} = \begin{cases} 1 & if \quad k = 0 \\ 0 & if \quad k > 0 \end{cases} \tag{1}$$

The first member of the formula expresses that only the newly arrived bits are to be transferred in the n-th time-slot, if the number of bits to be transferred was not greater than the K capacity threshold in the $(n-1)$-th time slot (because they were all transferred and no one remained waiting). The second member expresses that l bits remained waiting from the previous time-slot and $k-l$ is the number of the newly arrived bits. The question of convergence is formalized as follows: $\lim_{n\to\infty} p_k^{(n)} = ?$, and does a p_k^* limit distribution exist?

Let $\eta^{(n)}$ denote ***the number of bits transferred*** in the n-th time-slot:

$$\eta^{(n)} = \begin{cases} \zeta^{(n)}, & if \quad \zeta^{(n)} \le K \\ K \quad, & if \quad \zeta^{(n)} > K \end{cases} \tag{2}$$

3. Proof of Convergence

Theorem 1. *Let $\xi_1, \xi_2, \ldots \xi_n, \ldots$ be independent random variables following the same distribution: $\mathbb{E}(\xi)=m$, $\mathbb{D}(\xi)=\sigma$, $m<K$.*

$$\lim_{n\to\infty} \mathbb{P}(\xi_1 + \xi_2 + \ldots + \xi_n > nK) = 0 \tag{3}$$

That is, the probability of the event, that the length of the bitstream produced by the generator G within a period of nT exceeds the line capacity, converges to 0 if $n\to\infty$.

Proof: By the central limit distribution theorem:

$$\lim_{n\to\infty} \mathbb{P}\left(\frac{\xi_1 + \xi_2 + \ldots + \xi_n - nm}{\sigma\sqrt{n}} < x\right) = \Phi(x) \tag{4}$$

where $\Phi(x)$ is the cumulative density function of the standard normal distribution:

$$\Phi(x) = \frac{1}{\sqrt{2\pi}} \int_{t=-\infty}^{x} e^{-\frac{t^2}{2}} dt \tag{5}$$

$$\mathbb{P}(\xi_1 + \xi_2 + \ldots + \xi_n > nK) =$$
$$= \mathbb{P}\left(\frac{\xi_1 + \xi_2 + \ldots + \xi_n - nm}{\sigma\sqrt{n}} > \frac{nK - nm}{\sigma\sqrt{n}}\right) =$$
$$= \mathbb{P}\left(\frac{\xi_1 + \xi_2 + \ldots + \xi_n - nm}{\sigma\sqrt{n}} > \frac{\sqrt{n}}{\sigma}(K - m)\right)$$

Let $N>0$ be an arbitrary natural number. For for all N, there exists an n_0 so that if $n>n_0$ then $\frac{\sqrt{n}}{\sigma}(K-m) > N$. That is, if $n>n_0$ then:

$$\mathbb{P}\left(\frac{\xi_1 + \xi_2 + \ldots + \xi_n - nm}{\sigma\sqrt{n}} > \frac{\sqrt{n}}{\sigma}(K - m)\right) \le$$
$$\le \mathbb{P}\left(\frac{\xi_1 + \xi_2 + \ldots + \xi_n - nm}{\sigma\sqrt{n}} > N\right)$$

Now, let us consider the following inequality:

$$\lim_{n\to\infty} \mathbb{P}(\xi_1 + \xi_2 + \ldots + \xi_n > nK) =$$
$$= \lim_{n\to\infty} \mathbb{P}\left(\frac{\xi_1 + \xi_2 + \ldots + \xi_n - nm}{\sigma\sqrt{n}} > \frac{\sqrt{n}}{\sigma}(K - m)\right) \le$$
$$\le \lim_{n\to\infty} \mathbb{P}\left(\frac{\xi_1 + \xi_2 + \ldots + \xi_n - nm}{\sigma\sqrt{n}} > N\right) = 1 - \Phi(N)$$

Now, if $N\to\infty$ then $\Phi(N)\to 1$, that is: $\lim_{N\to\infty} (1-\Phi(N))=0$.

Theorem 2. *Using the conditions of Theorem 1, the probability of the event that there are waiting bits at the end of <u>all</u> the $T_1, T_2, \ldots, T_n$, intervals is likely to be 0, if $n\to\infty$. This can be expressed as follows:*

$$\lim_{n\to\infty} \mathbb{P}((\xi_1 > K) \wedge (\xi_1 + \xi_2 > 2K) \wedge \ldots$$
$$\ldots \wedge (\xi_1 + \xi_2 + \ldots + \xi_n > nK)) = 0 \tag{6}$$

Proof: The event above is <u>a subset of</u> the event that: $\xi_1 + \xi_2 + \ldots + \xi_n > nK$.
Therefore, it is true, that:

$$\mathbb{P}((\xi_1 > K) \wedge (\xi_1 + \xi_2 > 2K) \wedge \ldots$$
$$\ldots \wedge (\xi_1 + \xi_2 + \ldots + \xi_n > nK)) \le$$
$$\le \mathbb{P}(\xi_1 + \xi_2 + \ldots + \xi_n > nK)$$

$\mathbb{P}\left(\xi_1 + \xi_2 + ... + \xi_n > nK\right) \to 0$ if $n \to \infty$ (see Theorem 1). So we have shown, that:

$$\lim_{n \to \infty} \mathbb{P}\big((\xi_1 > K) \wedge (\xi_1 + \xi_2 > 2K) \wedge ...$$
$$... \wedge (\xi_1 + \xi_2 + ... + \xi_n > nK) \big) \le$$
$$\le \lim_{n \to \infty} \mathbb{P}\left(\xi_1 + \xi_2 + ... + \xi_n > nK\right) = 0$$

Corollary: *If m<K, then at least at the end of one of the intervals T_1, T_2, ..., T_n, if $n \to \infty$, there will be no waiting bits, with the probability of 1. When this event happens, we can consider it as if the process would start again from the beginning.*

Definition 1. *Let ξ_1 and ξ_2 be random variables. We say that ξ_1 is greater than ξ_2 by distribution, if for $\forall x \in \mathbb{R}$ it is true, that: $\mathbb{P}(\xi_1 \ge x) \ge \mathbb{P}(\xi_2 \ge x)$ and $\exists$ at least one x_0 that $\mathbb{P}(\xi_1 \ge x_0) > \mathbb{P}(\xi_2 \ge x_0)$. We shall denote this relation with the traditional 'greater than' sign between the 2 random variables: $\xi_1 > \xi_2$.*

Let us consider some features of this relation.

Theorem 3. *Let $F_1(x)$ and $F_2(x)$ denote the cumulative density function of random variables ξ_1 and ξ_2, respectively.*

$$\xi_1 > \xi_2 \iff F_1(x) \le F_2(x) \text{ and there is an } x_0,$$
$$\text{where } F_1(x_0) < F_2(x_0) \tag{7}$$

Proof is provided in two parts. The proof of the $\Rightarrow$ part: As $F_i(x) = \mathbb{P}(\xi_i < x) = 1 - \mathbb{P}(\xi_i \ge x)$ $(i=1,2)$ and from definition 1 it comes, that:

$$\mathbb{P}(\xi_1 \ge x) \ge \mathbb{P}(\xi_2 \ge x)$$
$$1 - F_1(x) \ge 1 - F_2(x)$$
$$F_2(x) \ge F_1(x)$$

And there is an x_0, where from $\mathbb{P}(\xi_1 \ge x_0) > \mathbb{P}(\xi_2 \ge x_0)$ comes that: $F_2(x_0) > F_1(x_0)$

The proof of the $\Leftarrow$ part is achieved by following the steps of the proof of the $\Rightarrow$ part in reverse direction.

Before further investigations, we introduce the distribution vectors.

Definition 2. *ξ is a non-negative discrete random variable, which can take natural numbers as its values. Let us use the following notations: $p_0 = \mathbb{P}(\xi=0)$, $p_1 = \mathbb{P}(\xi=1)$, ... $p_n = \mathbb{P}(\xi=n)$. The $\underline{p}(p_0, p_1, ... p_n, ...)$ distribution vector is a finite or infinite series, which satisfies*

$$\sum_{k=0}^{\infty} p_k = 1 \text{ and } p_k \ge 0 \text{ for } \forall k \in N. \tag{8}$$

To all $\underline{q}(q_0, q_1, ... q_n, ...)$ series, satisfying

$$\sum_{k=0}^{\infty} q_k = 1 \text{ and } q_k \ge 0 \text{ for } \forall k \in N \tag{9}$$

we can order a distribution so that $\underline{q}$ is the distribution vector of that distribution.

Theorem 4. *Let $\underline{p}(p_0, p_1, ... p_n, ...)$ and $\underline{q}(q_0, q_1, ... q_n, ...)$ be two distribution vectors.*

$$\underline{p} > \underline{q} \iff (p_0 \le q_0) \wedge (p_0 + p_1 \le q_0 + q_1) \wedge ...$$
$$\wedge (\text{for } \forall k \in N: \sum_{l=0}^{k} p_l \le \sum_{l=0}^{k} q_l) \wedge (\exists k_0 \in N: \tag{10}$$
$$\sum_{l=0}^{k_0} p_l < \sum_{l=0}^{k_0} q_l)$$

Proof: Trivial. Use Theorem 3 and observe the cumulative density function of $\underline{p}$ and $\underline{q}$:

$$F_{\underline{p}}(x) = \begin{cases} 0 & if & x \le 0 \\ p_0 & if & 0 < x \le 1 \\ p_0 + p_1 & if & 1 < x \le 2 \\ ... \\ \sum_{l=0}^{k} p_l & if & k < x \le k+1 \end{cases} \tag{11}$$

$$F_{\underline{q}}(x) = \begin{cases} 0 & if & x \le 0 \\ q_0 & if & 0 < x \le 1 \\ q_0 + q_1 & if & 1 < x \le 2 \\ ... \\ \sum_{l=0}^{k} q_l & if & k < x \le k+1 \end{cases} \tag{12}$$

Theorem 5. *Let us consider the following distribution vector series: $\underline{p}$; $\underline{p}_1$, $\underline{p}_2$, ... $\underline{p}_n$, where $\underline{p}$ is the distribution vector of ξ (that is: $\mathbb{P}(\xi=k)=p_k$) and $\underline{p}_1$, $\underline{p}_2$, ... $\underline{p}_n$ are the distribution vectors of $\zeta^{(1)}$, $\zeta^{(2)}$, ... $\zeta^{(n)}$, respectively. Now recall equation (1) from chapter 1. This equation defines the components $(p_1^{(n)}, p_2^{(n)}, ... p_k^{(n)}, ...)$ of the $\underline{p}_n$ distribution vector.*

$$\underline{p}_n > \underline{p}_{n-1} \text{ for } \forall n \in N^+ \tag{13}$$

Expressing in words: we face a strictly monotonously increasing series of distributions.

Proof: First, let us show, that $\underline{p}_1 > \underline{p}$:

$p_0^{(1)} = (p_0 + p_1 + ... + p_K)p_0 \le p_0$

(We can assume, that $\mathbb{P}(\xi > K) > 0$, otherwise there would never be waiting bits at all.)

$p_1^{(1)} = (p_0 + p_1 + ... + p_K)p_1 + p_{K+1}p_0$

$p_0^{(1)} + p_1^{(1)} = (p_0 + p_1 + ... + p_K)(p_0 + p_1) + p_{K+1}p_0 \le$
$(p_0 + p_1 + ... + p_K + p_{K+1})(p_0 + p_1) \le p_0 + p_1$ (O.K.)

In general:

$$\sum_{k=0}^{n} p_k^{(1)} = \sum_{k=0}^{n}\left(p_k \sum_{l=0}^{K} p_l + \sum_{l=1}^{k} p_{l+K} p_{k-l} \right) =$$

$$\left(\sum_{k=0}^{n} p_k\right)\left(\sum_{l=0}^{K} p_l\right) + \sum_{l=1}^{n} p_{l+K}\sum_{k=l}^{\infty} p_{k-l} \le \sum_{l=0}^{K} p_l + \sum_{l=1}^{n} p_{l+K} =$$

$$\sum_{l=0}^{n} p_l = \sum_{k=0}^{n} p_k \quad \text{(O.K.)}$$

If $\underline{p}$ has at least 2 non-zero elements and $\mathbb{P}(\xi > K) > 0$, than the "=" cannot always stand. So $\underline{p}_1 > \underline{p}$ was shown.

It can be shown in a similarly way that: $\underline{p}_n > \underline{p}_{n-1}$. In the general step, it is shown that:

$$\sum_{k=0}^{n} p_k^{(n)} \le \sum_{k=0}^{n} p_k^{(n-1)} \tag{14}$$

$$\sum_{k=0}^{n} p_k^{(n)} = \sum_{k=0}^{n}\left(p_k \sum_{l=0}^{K} p_l^{(n-1)} + \sum_{l=1}^{k} p_{l+K}^{(n-1)} p_{k-l} \right) =$$

$$\left(\sum_{k=0}^{n} p_k\right)\left(\sum_{l=0}^{K} p_l^{(n-1)}\right) + \sum_{l=1}^{n} p_{l+K}^{(n-1)}\sum_{k=l}^{\infty} p_{k-l} \le$$

$$\le \sum_{l=0}^{K} p_l^{(n-1)} + \sum_{l=1}^{n} p_{l+K}^{(n-1)} = \sum_{l=0}^{n} p_l^{(n-1)} = \sum_{k=0}^{n} p_k^{(n-1)} .$$

Theorem 6. *Let us consider again the following distribution vector series:*

$\underline{p} < \underline{p}_1 < \underline{p}_2 < ... < \underline{p}_n ...$

$$\lim_{n\to\infty} p_k^{(n)} = p_k^* \text{ for } \forall k \tag{15}$$

Proof: First, let us consider $k=0$. Then $p_0 \ge p_0^{(1)} \ge p_0^{(2)} \ge ... \ge p_0^{(n)} \ge ...$ is a monotonously decreasing series, that has a lower bound of *0*. According to Weierstrass Theorem, this series is convergent. $\lim_{n\to\infty} p_0^{(n)} = p_0^*$. Similarly, consider the following series:

$$p_0 + p_1 \ge p_0^{(1)} + p_1^{(1)} \ge p_0^{(2)} + p_1^{(2)} \ge ...$$
$$... \ge p_0^{(n)} + p_1^{(n)} \ge ...$$

This monotonously decreasing series has a lower bound of *0*, so it is also convergent. Let us denote its limes by α_1. Let us define p_1^* as follows: $p_1^* = \alpha_1 - p_0^*$. Because of the relationship between the limes and the addition operation ("+") it is true that: $\lim_{n\to\infty} p_1^{(n)} = p_1^*$

Similarly, if we have already shown, that the $\sum_{l=0}^{k} p_l^{(n)}$ $n=1, 2, ...$ series is convergent, then according to Weierstrass Theorem, the $\sum_{l=0}^{k+1} p_l^{(n)}$ $n=1, 2, ...$ series is

convergent (being a monotonously decreasing series with a lower bound *0*). Its limes is: $\alpha_{k+1} = \lim_{n\to\infty} \sum_{l=0}^{k+1} p_l^{(n)}$.

Let $p_{k+1}^* = \alpha_{k+1} - \sum_{l=0}^{k} p_l^*$, then $\lim_{n\to\infty} p_{k+1}^{(n)} = p_{k+1}^*$. (Ready)

Theorem 7. *Let us consider again the following distribution vector series:*

$\underline{p} < \underline{p}_1 < \underline{p}_2 < ... < \underline{p}_n ...$

$$\lim_{n\to\infty} \underline{p}_n = \underline{p}^*, \text{ where}$$
$$\underline{p}^* = \left(p_0^*; \quad p_1^*, \quad ... \quad p_k^*, \quad ...\right) \tag{16}$$

Proof: Besides the results of Theorem 6, we need to show, that: $\sum_{k=0}^{\infty} p_k^* = 1$

We use an induction for *n*:

n=0:

$$\sum_{k=0}^{\infty} p_k = 1$$

n=1:

$$\sum_{k=0}^{\infty} p_k^{(1)} = \sum_{k=0}^{\infty} p_k = 1$$

$n \to n+1$:

Using, that, $\sum_{k=0}^{\infty} p_k^{(n)} = 1$ is true for *n*, we show it for *n+1*:

$$\sum_{k=0}^{\infty} p_k^{(n+1)} = \sum_{k=0}^{\infty} p_k \sum_{l=0}^{K} p_l^{(n)} + \sum_{k=0}^{\infty} \sum_{l=1}^{k} p_{l+K}^{(n)} p_{k-l} =$$

$$= \sum_{l=0}^{K} p_l^{(n)} \sum_{k=0}^{\infty} p_k + \sum_{l=1}^{\infty} \sum_{k=l}^{\infty} p_{l+K}^{(n)} p_{k-l} =$$

$$= \sum_{l=0}^{K} p_l^{(n)} + \sum_{l=1}^{\infty} p_{l+K}^{(n)} \sum_{k=l}^{\infty} p_{k-l} = \sum_{l=0}^{K} p_l^{(n)} + \sum_{l=K+1}^{\infty} p_l^{(n)} =$$

$$\sum_{l=0}^{\infty} p_l^{(n)} = 1$$

That is, $\underline{p}^*$ is really a distribution vector.

4. Speed of Convergence

4.1. Examining the Speed of Convergence

Let us use a continuous approximation in the following instead of the discrete one!

We saw that the discrete model is convergent; therefore, the smaller time interval (T) we choose, the better the two models approximate each other. We can presume that the discrete model behaves similarly.

Let us suppose the amount of information produced is m bits in average in a unit of time.

The quantity of information transferred under a short [t, $t+\Delta t$] time interval is time proportionate and is equal to $g(t)\Delta t$ in average.

Let us suppose about our system that for small changes there is a linear relationship between the change of information transferred and the change of the amount of waiting information.

In this case the following equation can be written:

$$g(t+\Delta t)-g(t)=a(m\Delta t-g(t)\Delta t), \text{ where } a>0 \qquad (17)$$

From the equation above we get the differential equation:

$$g'(t)+ag(t)=am \qquad (18)$$

the solution of which is:

$$g(t)=m-(m-m_0)e^{-at}, \qquad (19)$$

where $g(0)=m_0$ and $g(t)$ is an exponential function, and $\lim_{t\to\infty} g(t) = m$.

In the solution there is a constant a describing the speed of convergence.

Next we determine the value of a.

For the quantity of information transferred in time-slot T_n the following equation can be set:

$$\mathbb{E}(\eta^{(n)}) \cong g(T_n)T = \left(m-\left(m-m_0\right)e^{-anT}\right)T \qquad (20)$$

From this equation a can be determined:

$$a = \frac{1}{nT}\ln\frac{(m-m_0)T}{mT-E(\eta^{(n)})} \qquad (21)$$

4.2. The Stopping Criterion

The quantity of information to be transferred in time interval T_n is:

$$\mathbb{E}(\zeta^{(n)}) = (n+1)Tm - \int_0^{nT} g(t)dt =$$

$$= (n+1)Tm - \int_0^{nT} m-(m-m_0)e^{-at}dt =$$

$$= Tm + \frac{1}{a}(1-e^{-anT})$$

It means that:

$$\mathbb{E}(\zeta^{(*)}) = \lim_{n\to\infty} \mathbb{E}(\zeta^{(n)}) = Tm + \frac{1}{a}$$

If we want

$$|\mathbb{E}(\zeta^{(n)}\text{-}\mathbb{E}\zeta^{(*)})| < \varepsilon \qquad (22)$$

to be true where ε is the error of approximation, then the following inequality must also stand:

$$n_\varepsilon > -\frac{1}{aT}\ln(\varepsilon a) \qquad (23)$$

Because the continuous model is only an approximation of the discrete model, we have to test the accuracy reached in practical problems.

When testing the results on computer, we found that the method provided a correct order of magnitude for the number of steps, but to determine n_ε a multiplier between 1,2 and 1,5 should be applied.

Conclusions

A mathematical model of the key algorithm of Traffic-Flow Analysis was set up. A formal proof for the convergence of the algorithm was presented by means of a series of theorems.

The speed of convergence of the algorithm was determined and the stopping criterion was also given.

We conclude that TFA has its solid mathematical foundations and can it be used as a method for fast performance estimation of communication systems.

Acknowledgements

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